HL First-Year Chemistry

1. Atomic Structure and Stoichiometry

Solutions to further problems:

- 1. (a) $_{26}^{55}$ Fe (b) $_{37}^{86}$ Rb (c) $_{81}^{123}$ Tl (d) $_{24}^{123}$ Cr
- 2. Introduction of the source, vaporization of the sample, ionization, acceleration, velocity selection, deflection, and detection.

3.
$$A_R (Ti) = \left(\frac{7.95}{100}\right) X 46 + \left(\frac{7.75}{100}\right) X 47 + \left(\frac{73.45}{100}\right) X 48 + \left(\frac{5.51}{100}\right) X 49 + \left(\frac{5.34}{100}\right) X 50$$

= 47.9254 = 47.9 or 48.

- 4. Relative atomic masses of some elements are so far off from whole numbers because it represents the average mass of multiple isotopes that make up the element.
- 5. (a) protons = 55, neutrons = 77, electrons = 55,
 - (b) protons = 48, neutrons = 67, electrons = 46,
 - (c) protons = 81, neutrons = 113, electrons = 81,
 - (d) protons = 47, neutrons = 58, electrons = 46,
 - (e) protons = 34, neutrons = 44, electrons = 36
- 6. The sample is first vaporized (into gaseous atoms) and then they are ionized, and then accelerated by a strong electric field into an area where they are further exposed to a varying magnetic or electric field ultimately reaching the detector where the charged ions are detected as electric current.
- 7. (a) 2 atoms of Na, 1 atom of C, and 3 atoms of O (b) 3 atoms of N, 12 of H, 1 of P and 4 of O (c) 3 atoms of Na, 1 of Ag, 4 of S, 6 of O
- 8. (a) 2 moles of Na atoms, 1 mole of C atoms, and 3 moles of O atoms (b) 3 moles of N atoms, 12 moles of H atoms, 1 mole of P atoms and 4 moles of O atoms (c) 3 moles of Na atoms, 1 mole of Ag atoms, 4 moles of S atoms, 6 moles of O atoms
- 9. Fe and CO₂ are the products. The equation is NOT balanced.
- 10. (a) Products: CaCl₂, CO₂ and H₂O, reactants: CaCO₃ and HCl
 - (b) equation is unbalanced.
 - (c) $CaCO_3 = solid$, HCl = aqueous, $CaCl_2 = aqueous$, $CO_2 = gas$, and $H_2O = liquid$
- 11. $HgS_{(s)} + O_{2(g)} \rightarrow Hg_{(l)} + SO_{2(g)}$
- 12. (a) there is no unit for relative molecular mass (b) g
- 13. (a) 60.06 g (b) 174.26 g (c) 74.10 g

14. a)
$$\left(\frac{55.85 \text{ g Fe}}{1 \text{ mol Fe}}\right) \left(\frac{1 \text{ mol Fe atoms}}{6.022 \text{ X } 10^{23} \text{ atoms of Fe}}\right) = 9.2743 \text{ X } 10^{-23} \text{ g Fe/atom of Fe}$$

=
$$9.274 \times 10^{-23}$$
 g Fe/atom of Fe (4 sig figs)

b) (5 X
$$10^{10}$$
 molecules N₂O) $\left(\frac{1 \text{ mol N}_2\text{O}}{6.022 \text{ X} 10^{23} \text{ molecules N}_2\text{O}}\right) \left(\frac{44.00 \text{ g N}_2\text{O}}{1 \text{ mol N}_2\text{O}}\right)$
= 3.65 X 10^{-12} g N₂O = 4 X 10^{-12} g N₂O (1 sig fig)

15. Percent composition of:

a) NH₃ (ammonia):
$$A_R$$
 (N) = 14.01, A_R (H) = 1.01
 M_R (NH₃) = 14.01 + 3(1.01) = 14.01 + 3.03 = 17.04 [2 decimal places]
% N = $\left(\frac{14.01}{17.04}\right)$ X 100 = 82.218 = 82.22 [4 sig. figs]

% H =
$$\left(\frac{3.03}{17.04}\right)$$
 X 100 = 17.781 = 17.8 [3 sig. figs.]

[**NB**: The total of the percent compositions add up to 100.02, which when rounded off to one decimal place—to be consistent with the percent composition of hydrogen—it comes out to 100.0.]

OR considering a mole of ammonia:

Mass of N in a mole of ammonia = 14.01 g

Mass of H in a mole of ammonia = 3 (1.01 g) = 3.03 g

Molar mass of ammonia = 17.04 g

% N =
$$\left(\frac{14.01 \,\mathrm{g}}{17.04 \,\mathrm{g}}\right)$$
 X 100 = 82.218 = 82.22 [4 sig. figs]

% H =
$$\left(\frac{3.03 \text{ g}}{17.04 \text{ g}}\right)$$
 X 100 = 17.781 = 17.8 [3 sig. figs.]

[**NB**: It makes no difference whether you determine percent compositions using relative mass or molar mass!]

b)
$$C_2H_4O_2$$
 (ethanoic acid): $A_R(C) = 12.01$, $A_R(H) = 1.01$, $A_R(O) = 16.00$

 $M_R (C_2H_4O_2) = 2(12.01) + 4(1.01) + 2(16.00) = 60.06$ [2 decimal places]

% C =
$$\left(\frac{24.02}{60.06}\right)$$
 X 100 = 39.99 [4 sig. figs.]

% H =
$$\left(\frac{4.04}{60.06}\right)$$
 X 100 = 6.73 [3 sig. figs.]

% O =
$$\left(\frac{32.00}{60.06}\right)$$
 X 100 = 53.28 [4 sig. figs.]

c)
$$K_2SO_4$$
 (potassium sulfate): $A_R(K) = 39.10$, $A_R(S) = 32.06$, $A_R(O) = 16.00$

formula mass $(K_2SO_4) = 2(39.10) + 32.06 + 4(16.00) = 174.26$ [2 decimal places]

% K =
$$\left(\frac{78.20}{174.26}\right)$$
 X 100 = 44.88 [4 sig. figs.]

% S =
$$\left(\frac{32.06}{174.26}\right)$$
 X 100 = 18.40 [4 sig. figs.]

% O =
$$\left(\frac{64.00}{174.26}\right)$$
 X 100 = 36.73 [4 sig. figs.]

d)
$$Ca(OH)_2$$
: A_R (Ca) = 40.08, A_R (O) = 16.00, A_R (H) = 1.01

formula mass $(Ca(OH)_2) = 74.10$ [2 decimal places]

% Ca =
$$\left(\frac{40.08}{74.10}\right)$$
 X 100 = 54.09 [4 sig. figs.]

% O =
$$\left(\frac{32.00}{74.10}\right)$$
 X 100 = 43.18 [4 sig. figs.]

% H =
$$\left(\frac{2.02}{74.10}\right)$$
 X 100 = 2.73 [3 sig. figs.]

(e) $Zn(NO_3)_2 \bullet 6H_2O$:

formula mass = 297.51 [2 decimal places]

% Zn =
$$\left(\frac{65.37}{297.51}\right)$$
 X 100 = 21.97 [4 sig. figs.]

% N =
$$\left(\frac{28.02}{297.51}\right)$$
 X 100 = 9.418 [4 sig. figs.]

% O =
$$\left(\frac{192.00}{297.51}\right)$$
 X 100 = 64.536 [5 sig. figs.]
% H = $\left(\frac{12.12}{297.51}\right)$ X 100 = 4.074 [4 sig. figs.]

[**NB**: The sum of the percentages adds up to 99.998 which when rounded off to 2 decimal places,

which is what you have to do since the percentage of zinc is correct only to 2 decimal place, the

sum does result in 100.]

f) C₂₂H₂₀O₁₂N₇

$$M_{R} (C_{22}H_{20}O_{12}N_{7}) = 574.49$$
% $C = \left(\frac{264.22}{574.49}\right) X 100 = 45.992 [5 \text{ sig. figs.}]$
% $H = \left(\frac{20.20}{574.49}\right) X 100 = 4.516 [4 \text{ sig. figs.}]$
% $O = \left(\frac{192.00}{574.49}\right) X 100 = 33.421 [5 \text{ sig. figs.}]$
% $N = \left(\frac{98.07}{574.49}\right) X 100 = 17.07 [4 \text{ sig. figs.}]$

16. a) 1.00 lb NH₃
$$\left(\frac{1 \text{ kg NH}_3}{2.2 \text{ lb NH}_3}\right) \left(\frac{1000 \text{ g NH}_3}{1 \text{ kg NH}_3}\right) \left(\frac{1 \text{ mol NH}_3}{17.04 \text{ g NH}_3}\right) = 26.7 \text{ mol NH}_3 [3 \text{ sig figs}]$$

b)
$$1.00 \text{ lb } C_2H_4O_2 \left(\frac{1 \text{ kg } C_2H_4O_2}{2.2 \text{ lb } C_2H_4O_2}\right) \left(\frac{1000 \text{ g } C_2H_4O_2}{1 \text{ kg } C_2H_4O_2}\right) \left(\frac{1 \text{ mol } C_2H_4O_2}{60.06 \text{ g } C_2H_4O_2}\right) = 7.50 \text{ mol } C_2H_4O_2 [3]$$

sig figs]

c)
$$1.00 \text{ lb } \text{K}_2 \text{SO}_4 \left(\frac{1 \text{kg K}_2 \text{SO}_4}{2.2 \text{ lb K}_2 \text{SO}_4} \right) \left(\frac{1000 \text{ g K}_2 \text{SO}_4}{1 \text{ kg K}_2 \text{SO}_4} \right) \left(\frac{1 \text{mol K}_2 \text{SO}_4}{174.26 \text{ g K}_2 \text{SO}_4} \right) = 2.61 \text{ mol K}_2 \text{SO}_4 \text{ [3 signifies]}$$

d)
$$1.00 \text{ lb Ca(OH)}_2 \left(\frac{1 \text{ kg Ca(OH)}_2}{2.2 \text{ lb Ca(OH)}_2} \right) \left(\frac{1000 \text{ g Ca(OH)}_2}{1 \text{ kg Ca(OH)}_2} \right) \left(\frac{1 \text{ mol Ca(OH)}_2}{74.10 \text{ g Ca(OH)}_2} \right) = 6.13 \text{ mol}$$

Ca(OH)₂

[3 sig figs]

e)
$$1.00 \text{ lb } Zn(NO_3)_2 \bullet 6H_2O\left(\frac{1 \text{ kg } Zn(NO_3)_2 \bullet 2H_2O}{2.2 \text{ lb } Zn(NO_3)_2 \bullet 2H_2O}\right) \left(\frac{1000 \text{ g } Zn(NO_3)_2 \bullet 2H_2O}{1 \text{ kg } Zn(NO_3)_2 \bullet 2H_2O}\right)$$

$$\left(\frac{1 \text{ mol } Zn(NO_3)_2 \bullet 2H_2O}{297.51 \text{ g } Zn(NO_3)_2 \bullet 2H_2O}\right) = 1.53 \text{ mol } Zn(NO_3)_2 \bullet 2H_2O \text{ [3 sig figs]}$$

f) 1.00 lb
$$C_{22}H_{20}O_{12}N_7 \left(\frac{1 \text{ kg } C_{22}H_{04}O_{12}N_7}{2.2 \text{ lb } C_{22}H_{04}O_{12}N_7}\right) \left(\frac{1000 \text{ g } C_{22}H_{04}O_{12}N_7}{1 \text{ kg } C_{22}H_{04}O_{12}N_7}\right) \left(\frac{1 \text{ mol } C_{22}H_{04}O_{12}N_7}{574.49 \text{ g } C_{22}H_{04}O_{12}N_7}\right)$$

$$= 0.791 \text{ mol } C_2H_4O_2 \text{ [3 sig figs]}$$

17. (a)
$$(15.4 \text{ g Al}) \left(\frac{1 \text{ mol Al}}{26.98 \text{ g Al}} \right) \left(\frac{6.022 \times 10^{23} \text{ atoms Al}}{1 \text{ mol Al}} \right) = 3.43 \times 10^{23} \text{ atoms Al (3 sig figs)}$$

(b)
$$(14.8 \text{ g N}_2\text{O}_5) \left(\frac{1 \text{ mol N}_2\text{O}_5}{108.00 \text{ g N}_2\text{O}_5} \right) \left(\frac{6.022 \text{ X} 10^{23} \text{ molecules N}_2\text{O}_5}{1 \text{ mol N}_2\text{O}_5} \right)$$

= 8.25 X 10²² molecules of N₂O₅
(c) $(83.2 \text{ g Na}_2\text{CO}_3) \left(\frac{1 \text{ mol Na}_2\text{CO}_3}{105.99 \text{ g Na}_2\text{CO}} \right) \left(\frac{2 \text{ mol Na ions}}{1 \text{ mol Na ions}} \right) \left(\frac{6.022 \text{ X} 10^{23} \text{ Na ions}}{1 \text{ mol Na ions}} \right)$

18. (7 mol C)
$$\left(\frac{1 \operatorname{mol} C_3 H_8 O_3}{3 \operatorname{mol} C}\right) \left(\frac{3 \operatorname{mol} O}{1 \operatorname{mol} C_3 H_8 O_3}\right) = 7 \operatorname{mol} O$$
, which you should have been able to

determine without even setting it up as shown above. Since in a mole of glycerol the number of moles of C and O are equal (3:3) any sample of glycerol would have equal number of moles of C and O.

19. Equation is: $2Cu_{(s)} + S_{(aq)} \rightarrow Cu_2S_{(s)}$

$$(100.0 \text{ g Cu}) \left(\frac{1 \text{ mol Cu}}{63.55 \text{ g Cu}} \right) \left(\frac{1 \text{ mol S}}{2 \text{ mol Cu}} \right) \left(\frac{32.06 \text{ g S}}{1 \text{ mol S}} \right) = 25.224 = 25.22 \text{ g S}$$

Limiting reagent is copper

$$(100.0 \text{ g Cu}) \left(\frac{1 \text{ mol Cu}}{63.55 \text{ g Cu}} \right) \left(\frac{1 \text{ mol Cu}_2\text{S}}{2 \text{ mol Cu}} \right) \left(\frac{159.16 \text{ g Cu}_2\text{S}}{1 \text{ mol Cu}_2\text{S}} \right) = 125.22 = 125.2 \text{ g. (4 sig figs)}$$

20. Equation is: $C_{(s)} + 2Cl_{2(g)} \rightarrow CCl_{4(l)}$

$$(10.0 \text{ g C}) \left(\frac{1 \text{ mol C}}{12.01 \text{ g C}} \right) \left(\frac{2 \text{ mol Cl}_2}{1 \text{ mol C}} \right) \left(\frac{70.90 \text{ g Cl}_2}{1 \text{ mol Cl}_2} \right) = 59.0 \text{ Cl}_2$$

Limiting reagent is carbon.

$$(10.0 \text{ g C}) \left(\frac{1 \text{ mol C}}{12.01 \text{ g C}}\right) \left(\frac{1 \text{ mol CCl}_4}{1 \text{ mol C}}\right) \left(\frac{141.80 \text{ g CCl}_4}{1 \text{ mol CCl}_4}\right) = 118.0 = 118 \text{ g CCl}_4 (3 \text{ sig figs})$$

Mass of excess reagent left unreacted = 100.0 g - 59.0 g = 41.0 g

21. The equation for the reaction is: $4Fe_{(s)} + 3O_{2(g)} \rightarrow 2Fe_2O_{3(s)}$

$$(4.80 \text{ g O}_2) \left(\frac{1 \text{ mol O}_2}{32.00 \text{ g O}_2} \right) \left(\frac{4 \text{ mol Fe}}{3 \text{ mol O}_2} \right) \left(\frac{55.85 \text{ g Fe}}{1 \text{ mol Fe}} \right) = 11.17 \text{ g Fe} = 11.2 \text{ g Fe} \text{ (required)}$$

$$(0.150 \text{ mol Fe}) \left(\frac{55.85 \text{ g Fe}}{1 \text{ mol Fe}} \right) = 8.3775 \text{ g Fe} = 8.38 \text{ g Fe} \text{ (available)}$$

Therefore, limiting reagent is Fe

$$(0.150 \text{ mol Fe}) \left(\frac{2 \text{ mol Fe}_2 O_3}{4 \text{ mol Fe}}\right) \left(\frac{159.70 \text{ g Fe}_2 O_3}{1 \text{ mol Fe}_2 O_3}\right) = 11.977 \text{ g Fe}_2 O_3 = 12.0 \text{ g Fe}_2 O_3 \text{ (produced)}$$

Mass of Fe remaining = 0

(0.150 mol Fe)
$$\left(\frac{3 \text{ mol O}_2}{4 \text{ mol Fe}}\right) \left(\frac{16.00 \text{ g O}_2}{1 \text{ mol O}_2}\right) = 1.8 \text{ g O}_2 = 1.80 \text{ g O}_2$$

Mass of oxygen remaining = 4.80 - 1.80 = 3.00 g (2 dp)

- 22. (a) NH₂SO₄, (b) CH, (c) C₃H₈O₃, (d) Hg₂SO₄.
- 23. Molecular Empirical formula
 - a) $C_3H_7O_2$ $C_3H_7O_2$
 - b)CH₄O CH₄O
 - c) C₄H₈O₂ C₂H₄O
 - d) C_2H_6O C_2H_6O

e)
$$C_2H_7N$$
 $C_2H_6O_2$ CH_3O

24. Tungsten Oxygen

Mass ratio 4.23 g $5.34 - 4.23 = 1.11$ g

Molar ratio 4.23 g $\frac{1 \text{ mol}}{183.85 \text{ g}} = 0.02300$ mol 1.11 g $\frac{1 \text{ mol}}{16.00 \text{ g}} = 0.06937$ mol Dividing by the smaller of the two numbers (to get whole number ratios) $\frac{0.02300}{0.02300} = 1$ $\frac{0.06937}{0.02300} = 3.016 \approx 3$

Therefore the empirical formula is WO₃.

25. a) C O Percentage 27.3% 72.7% 57.1 g Molar ratio
$$(42.9 \text{ g}) \left(\frac{1 \text{ mol}}{12.01 \text{ g}}\right) = 3.57 \text{ mol}$$
 $(57.1 \text{ g}) \left(\frac{1 \text{ mol}}{16.00 \text{ g}}\right) = 3.57 \text{ mol}$ Number of moles of O that $\left(\frac{3.57}{3.57}\right) = 1$ $\left(\frac{3.57}{3.57}\right) = 1$

Therefore the empirical formula is CO.

- b) CO₂ c) NaSO₄ d) Na₂S₂O₃.
- 26. There are a couple of different ways of tackling these kinds of questions.

Method A. The following is the long version with explanations. And it uses the stoichiometric ratio between the anhydrous salt and the hydrated form.

What the solution boils down to is determination of the number of moles of water produced by a mole of the hydrate knowing each of the moles of water and that of the hydrate in the sample of hydrate analyzed.

a) NiSO₄•
$$x$$
H₂O_(s) \rightarrow NiSO_{4(s)} + x H₂O_(g) residue = NiSO_{4(s)}

$$0.306 \text{ g NiSO}_4 \left(\frac{1 \text{ mol NiSO}_4}{154.77 \text{ g NiSO}_4} \right) = 0.001977 \text{ mol NiSO}_4$$

Since 1 mole of NiSO₄•xH₂O produces 1 mole of NiSO₄, number of moles of NiSO₄•xH₂O in the

original sample = number of moles of NiSO₄ produced = 0.001977.

Since the original mass was 0.520 g, then the mass of 1 mole of NiSO₄•xH₂O is given by:

$$\left(\frac{0.520 \text{ g NiSO}_4 \bullet \text{xH}_2\text{O}}{0.001977 \text{ mol NiSO}_4 \bullet \text{xH}_2\text{O}}\right) = 263 \text{ g/mol NiSO}_4 \bullet \text{xH}_2\text{O}$$

Mass of water in 1 mole of NiSO₄•xH₂O = molar mass of NiSO₄•xH₂O – molar mass of NiSO₄ (since molar ratio of NiSO₄•xH₂O: NiSO₄= 1:1)

$$= 263 - 154.77 = 108 g$$

Number of moles of water in 108 g of water = 108 g $H_2O\left(\frac{1 \text{ mol } H_2O}{18.02 \text{ g } H_2O}\right) = 5.99 = 6$

Therefore, x = 6. That is, in every mole of NiSO₄•xH₂O, there are 6 moles of water molecules.

Method B. This method uses the relationship between the products:

What the solution boils down to is determination of the number of moles of water produced for every mole of the anhydrous salt produced knowing each of the moles of water and that of the anhydrous salt in the sample of hydrate analyzed.

From the equation, the ratio of the products NiSO₄ to $H_2O = 1$ to x

That is,
$$\left(\frac{\text{moles of NiSO}_4}{\text{moles of H}_2\text{O}}\right) = \left(\frac{1 \text{ mole of NiSO}_4}{x}\right)$$

The ratio of $\left(\frac{\text{moles of NiSO}_4}{\text{moles of H}_2O}\right)$ in the experiment must also be the same.

Therefore.

$$\left(\frac{\text{experimental moles of NiSO}_4}{\text{experimental moles of H}_2\text{O}}\right) = \left(\frac{1 \, \text{mole of NiSO}_4}{x}\right) \quad \text{(Equation I)}$$

Moles of NiSO₄ produced in the experiment

$$0.306 \text{ g NiSO}_4 \left(\frac{1 \text{ mol NiSO}_4}{154.77 \text{ g NiSO}_4} \right) = 0.001978 \text{ mol NiSO}_4$$

Mass of water in the experiment = (0.520 - 0.306) g = 0.214 g

Moles of H₂O produced in the experiment:

$$0.214 \text{ g H}_2\text{O}\left(\frac{1 \text{ mol H}_2\text{O}}{18.02 \text{ g H}_2\text{O}}\right) = 0.0118 \text{ mol H}_2\text{O}$$

Substituting in equation I, and solving for x,

$$\left(\frac{0.00198 \text{ mole NiSO}_4}{0.0118 \text{ mole H}_2\text{O}}\right) = \left(\frac{1 \text{ mole of NiSO}_4}{x}\right)$$

$$\Rightarrow x = (1 \text{ mole of NiSO}_4) \left(\frac{0.0118 \text{ mole H}_2\text{O}}{0.00198 \text{ mole of NiSO}_4} \right) = 5.95 \text{ mol H}_2\text{O} = 6 \text{ mole H}_2\text{O}$$

b)
$$MnI_2 \bullet xH_2O_{(s)} \rightarrow MnI_{2(s)} + xH_2O_{(s)}$$

b)
$$MnI_2 \bullet xH_2O_{(s)} \rightarrow MnI_{2(s)} + xH_2O_{(g)}$$

 $x = (1 \text{ mole of } MnI_2) \left(\frac{\text{moles of } H_2O \text{ produced}}{\text{moles of } MnI_2 \text{ produced}} \right)$

Mass of water produced = (0.895 - 0.726) g = 0.169 g

$$0.169 \text{ g H}_2\text{O}\left(\frac{1 \text{ mol H}_2\text{O}}{18.02 \text{ g H}_2\text{O}}\right) = 0.00937 \text{ mol H}_2\text{O}$$

Moles of MnI₂ produced

$$0.726 \text{ g MnI}_2 \left(\frac{1 \text{ mol MnI}_2}{308.74 \text{ g MnI}_2} \right) = 0.00235 \text{ mol MnI}_2$$

$$x = (1 \text{ mole of MnI}_2) \left(\frac{0.00937 \text{ moles of H}_2\text{O}}{0.00235 \text{ moles of MnI}_2} \right) = 3.98 \text{ mol H}_2\text{O} = 4 \text{ mol H}_2\text{O}$$

c) similar to the ones above.

$$MgSO_4 \bullet xH_2O_{(s)} \rightarrow MgSO_{4(s)} + xH_2O_{(g)}$$

d) similar to the ones above.

$$CdSO_4 \bullet xH_2O_{(s)} \rightarrow CdSO_{4(s)} + xH_2O_{(g)}$$

e) Similar to the ones above.

$$KAl(SO_4)_2 \bullet xH_2O_{(s)} \rightarrow KAl(SO_4)_{2(s)} + xH_2O_{(g)}$$

27. Compound +
$$O_{2(g)} \rightarrow H_2O_{(g)} + CO_{2(g)}$$

Mass of compound = 12.13 mg

Mass of H_2O produced = 5.36 mg

Mass of hydrogen in the sample of water produced

5.36 mg H₂O
$$\left(\frac{1 \text{ g H}_2\text{O}}{1000 \text{ mg H}_2\text{O}}\right) \left(\frac{1 \text{ mol H}_2\text{O}}{18.02 \text{ g H}_2\text{O}}\right) \left(\frac{2 \text{ mol H}}{1 \text{ mol H}_2\text{O}}\right) \left(\frac{1.01 \text{ g H}}{1 \text{ mol H}}\right) = 0.000601 \text{ g H}$$

Mass of CO_2 produced = 30.6 mg

Mass of carbon in the carbon dioxide produced

$$30.6 \text{ mg CO}_2 \left(\frac{1 \text{ g CO}_2}{1000 \text{ mg CO}_2} \right) \left(\frac{1 \text{ mol CO}_2}{44.01 \text{ g CO}_2} \right) \left(\frac{1 \text{ mol C}}{1 \text{ mol CO}_2} \right) \left(\frac{12.01 \text{ g C}}{1 \text{ mol C}} \right) = 0.00835 \text{ g C}$$

Since all the hydrogen in water and carbon in carbon dioxide came from the original organic compound, the mass of hydrogen in the original compound = 0.000601 g, and mass of carbon in the

original compound = 0.00835 g.

Therefore,

mass of oxygen in the original compound =
$$0.01213 \text{ g} - (0.000601 + 0.00835) \text{ g}$$

= $0.01213 \text{ g} - 0.00895 \text{ g}$
= 0.00318 g

 $C \qquad \qquad H \qquad \qquad O$ Mass ratio \quad 0.00835 \quad 0.000601 \quad g \quad 0.00318 \quad g
Molar ratio \quad (0.00835 \quad g)\left(\frac{1\text{mol}}{12.01 \quad g}\right) \quad (0.000601 \quad g)\left(\frac{1\text{mol}}{1.01 \quad g}\right) \quad (0.00318

$$= 0.0006952 \text{ mol} = 0.0005950 \text{ mol} = 0.0001987 \text{ mol}$$

$$\frac{\text{Moles of C and}}{\text{H that combines}} \left(\frac{0.0006952}{0.0001987} \right) = 3.498 \qquad \left(\frac{0.0005950}{0.0001987} \right) = 2.994 \qquad \left(\frac{0.0001987}{0.0001987} \right) = 1$$
with 1 mol of O

Multiplying by 2
$$3.498 \text{ X } 2 = 6.996 \approx 7$$
 $2.994 \text{ X } 2 = 5.988 \approx 6$ $1 \text{ X } 2 = 2$

Therefore, the empirical formula is $C_7H_6O_2$.

28. Out of 100.0 g compound: 30.4 g N
$$\left(\frac{1 \text{ mol N}}{14.01 \text{ g N}}\right) = 2.17 \text{ mol N}$$

% O = 100.0 - 30.4 = 69.6%
69.6 g O $\left(\frac{1 \text{ mol O}}{16.00 \text{ g O}}\right) = 4.35 \text{ mol O}$

Number of moles of O per mol of N =
$$\frac{4.35}{2.17}$$
 = 2.00

Empirical formula = NO_2

Empirical formula mass = 14.01 + 2(16.00) = 46.01 g/mol

$$\frac{92 \text{ g}}{46.01 \text{ g}} = 2.0 \text{ ;}$$

Therefore, the molecular formula is N₂O₄.

29. Assuming 100.00 g of compound

Mass of hydrogen = 100.00 - 49.31 - 43.79 = 6.90 g

49.31 g C
$$\left(\frac{1 \text{ mol C}}{12.01 \text{ g C}}\right)$$
 = 4.106 mol C; 43.79 g O $\left(\frac{1 \text{ mol O}}{16.00 \text{ g O}}\right)$ = 2.737 mol O;

$$6.90 \text{ g H} \left(\frac{1 \text{ mol H}}{1.01 \text{ g H}} \right) = 6.83 \text{ mol H}$$

Dividing all mole values by 2.737 to get the number of moles of C and H per mole of O

$$\frac{4.106}{2.737}$$
 = 1.500 C; $\frac{6.83}{2.737}$ = 2.495 H

Multiplying the ratio by 2 yields whole number ratios givening an empirical formula C₃H₅O₂.

Empirical formula mass = 3(12.01) + 5(1.01) + 2(16.00) = 73.08 g/mol

$$\frac{\text{molar mass}}{\text{empirical formula mass}} = \frac{146.1}{73.08} = 1.999 = 2.00$$

Therefore, the molecular formula is $C_6H_{10}O_4$.

30. Assuming 100.00 g of compound

Mass of oxygen = 100.00 - 41.39 - 3.47 = 55.14 g

41.39 g C
$$\left(\frac{1 \text{ mol C}}{12.01 \text{ g C}}\right)$$
 = 3.446 mol C; 55.14 g O $\left(\frac{1 \text{ mol O}}{16.00 \text{ g O}}\right)$ = 3.446 mol O;

$$3.47 \text{ g H} \left(\frac{1 \text{ mol H}}{1.01 \text{ g H}} \right) = 3.435 \text{ mol H}$$

All three are the same mole values, therefore the empirical formula is CHO.

Empirical formula mass = 12.01 + 1.01 + 16.00 = 29.02 g/mol

Molar mass of compound =
$$\frac{15.0 \text{ g}}{0.129 \text{ mol}} = 116 \text{ g/mol}$$

$$\frac{\text{molar mass}}{\text{empirical formula mass}} = \frac{116}{29.02} = 4.00$$

Therefore, the molecular formula is C₄H₄O₄.